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INFORMATION SCIENCE AND TECHNOLOGY

Deformation rate estimation on  
**changing landscapes** using  
Temporarily Coherent Point InSAR

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THE HONG KONG  
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→ FRINGE 2011 WORKSHOP

# Deformation rate estimation on changing landscapes using Temporarily Coherent Point InSAR

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19-23 September 2011 | ESA-ESRIN | Frascati (Rome), Italy

European Space Agency

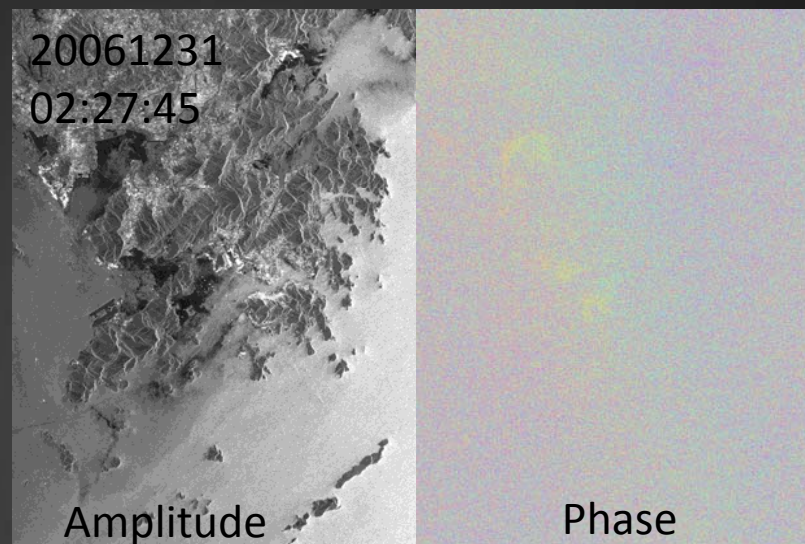
# Background

SAR data: single look complex (SLC)

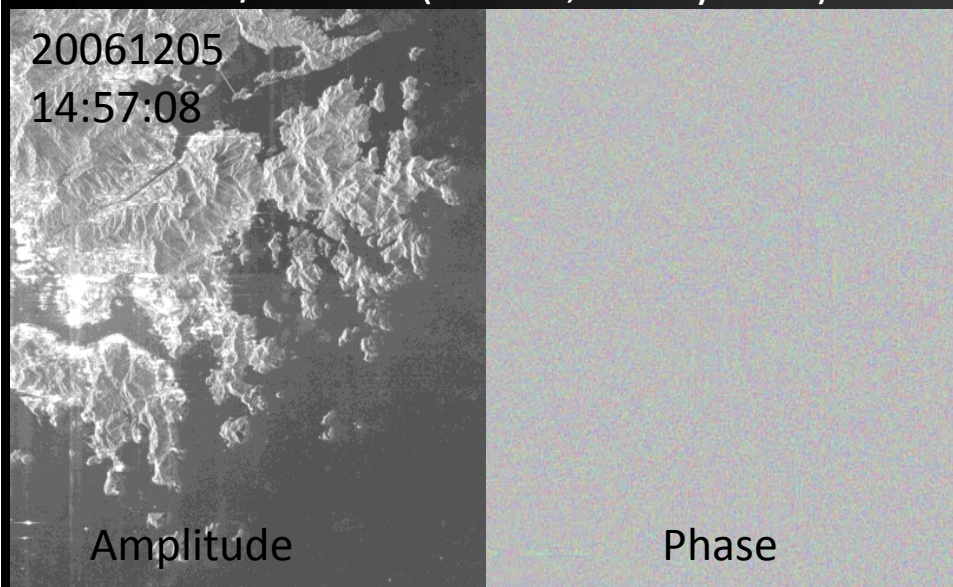
Amplitude      Phase

All-weather day/night imagery  
For a single SLC image, phase is useless...

Envisat/ASAR (C-band, 5m-by-25m)



ALOS/PALSAR (L-band, 3m-by-10m)



COSMO-SkyMed (X-band, 1m-by-1m)



# Background

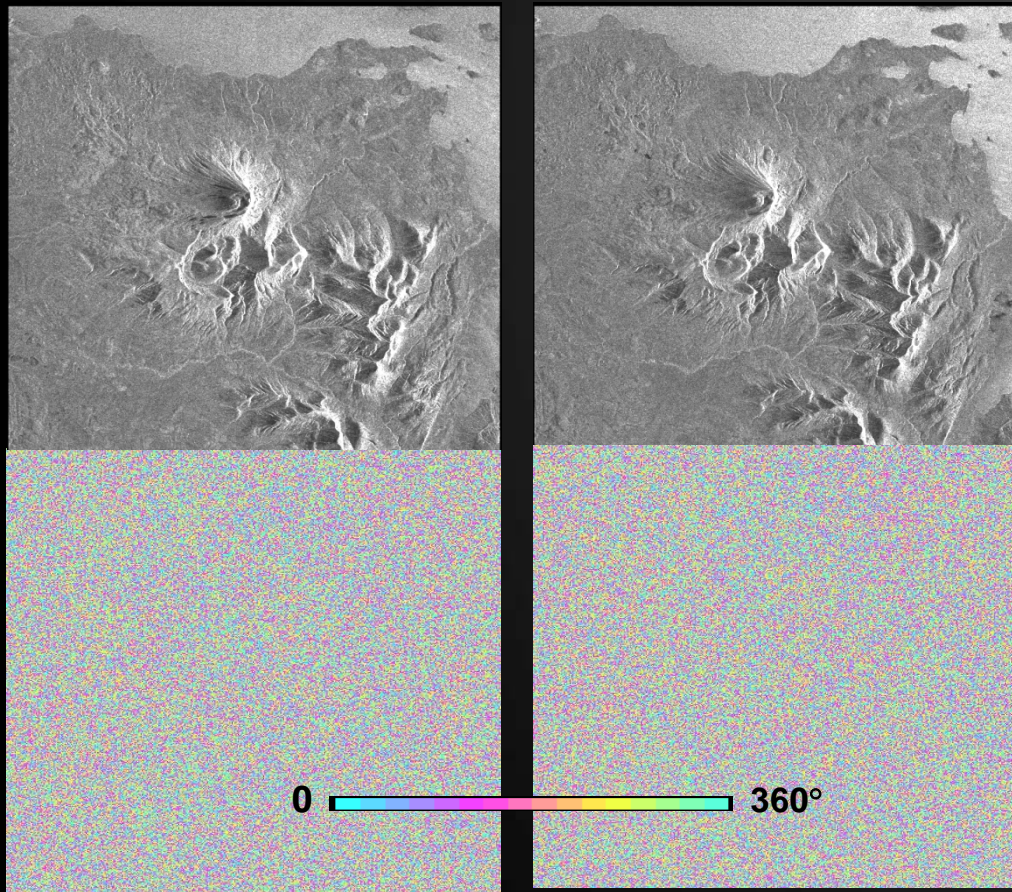
## SAR data: application

- >> Monitoring sea ice zones and the arctic environment
- >> Surveillance of marine environment (e.g. oil spill monitoring)
- >> Maritime security (e.g. ship detection)
- >> Wind, wave, current monitoring
- >> **Monitoring of land surface motion (subsidence, landslide, tectonics, volcanoes, etc.)**
- >> Support to emergency/risk management (e.g. flooding etc.)
- >> Mapping of land surface: forest, water and soil, agriculture, etc.

(source: ESA's GMES program)

# Background

## InSAR : phase analysis technique



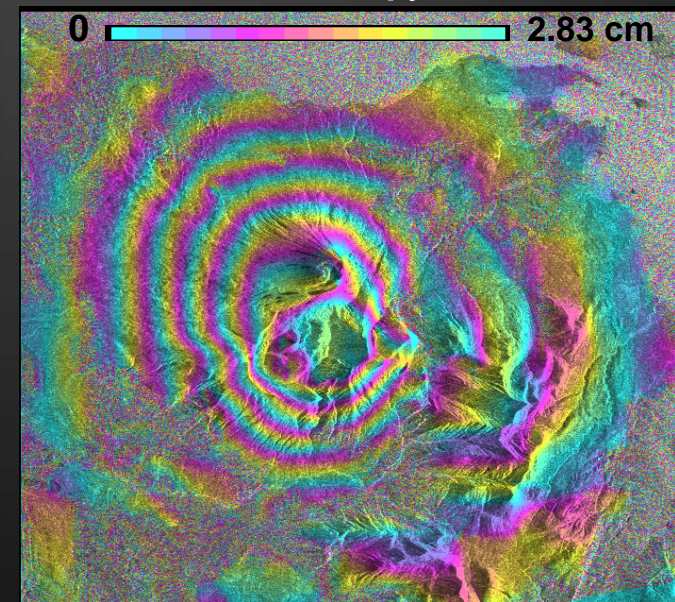
$$\phi_1 = -\frac{4\pi}{\lambda}r_1 + a_1$$

$$\phi_2 = -\frac{4\pi}{\lambda}r_2 + a_2$$

$$\phi = \phi_1 - \phi_2 = -\frac{4\pi(r_1 - r_2)}{\lambda} + (a_1 - a_2)$$

If  $a_1 = a_2 \dots$

$$\phi = \phi_1 - \phi_2 = -\frac{4\pi(r_1 - r_2)}{\lambda}$$



Interferometric phase is useful!!

# Background

**InSAR** : phase analysis technique

$$\phi = \phi_1 - \phi_2 = -\frac{4\pi(r_1 - r_2)}{\lambda} \iff \text{Target height and target motion}$$

$$\phi_{l,m}^i = \phi_{topo,l,m}^i + \phi_{defo,l,m}^i + \phi_{atmo,l,m}^i + \phi_{orbit,l,m}^i + \phi_{noise,l,m}^i$$

**InSAR** : precision (deformation) 1cm~ several cm

**Advanced InSAR** : multi-temporal InSAR technique

- Analysis of a large set of SAR images
- Focus on persistently coherent points
- Product: deformation rate & deformation time series
- Precision: **1mm~several mm**

# Background

**Advanced InSAR** : limitations of current techniques

-- phase unwrapping: low efficiency and/or unreliable

It has been solved by **TCPIInSAR** that can avoid phase unwrapping!!

-- dependence on persistently coherent points

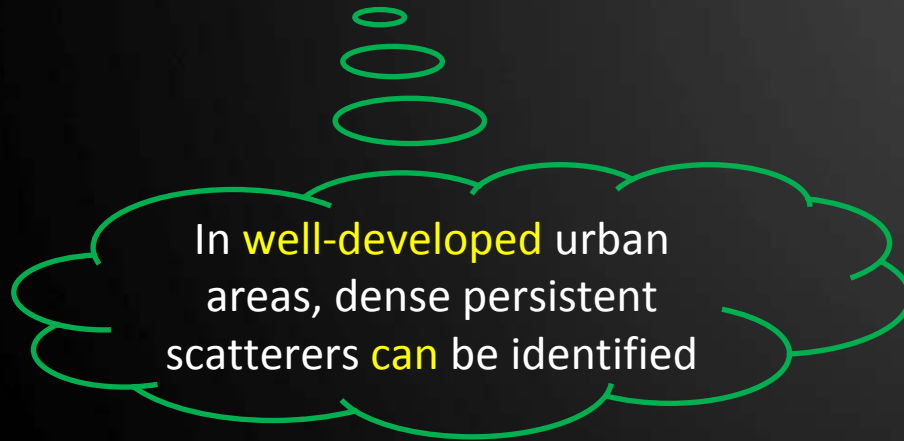
Current advanced InSAR techniques work well on stable landscapes

How about on changing landscapes?

# Background

## Stable vs. Changing Landscapes

on **stable landscapes** there are abundant scatterers that **can** keep visible during a long observation time span



1954

1985

2009

New York





# Background

## Stable vs. Changing Landscapes

However on **changing landscapes** there are abundant scatterers that **cannot** keep visible during a long observation time span

In **developing** urban areas, persistent scatterers **cannot** be densely identified

Dubai

1990



2003



2007

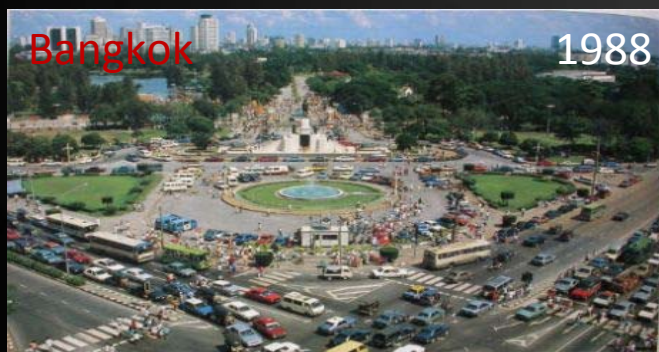


# Background

Most developing countries are undergoing surprisingly fast urbanization...

Townscapes have changed significantly, raising difficulties for current MT-InSAR techniques to get detailed defo. maps...

Urban renewal and sprawl...



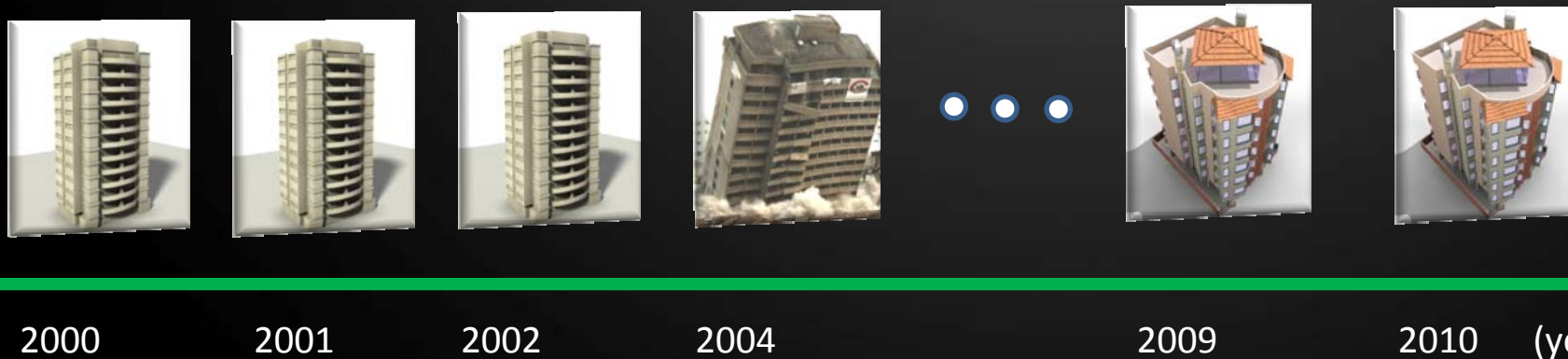
# Background

Persistently Coherent Point vs. Partially Coherent Point

Persistently Coherent Point – **Visible over the whole observation time span**



Partially Coherent Point – **Visible over a part of observation time span**



## Background



Can we identify both persistently coherent points and partially coherent points simultaneously and retrieve deformation from these points?

# Temporarily Coherent Point InSAR

## Temporarily Coherent Point

- not necessary to keep coherent during the whole time span
- including persistently coherent point and partially coherent point

## TCPInSAR

### TCP Identification

- >> image pair based method (offset deviation<sup>#</sup>)
- >> image based method (amplitude mad median ratio (AMMR) )

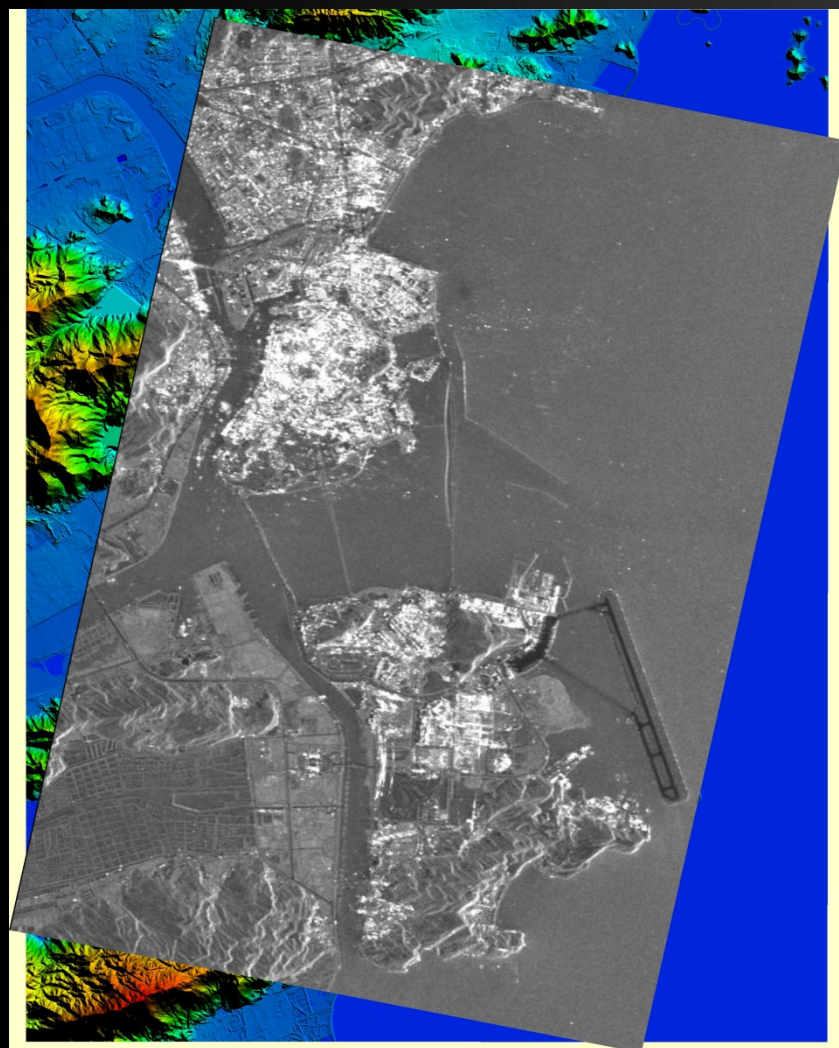
### Deformation estimation

- >> L2 norm (least squares) estimator with phase ambiguity detector\*
- >> L1 norm estimator

#: Zhang, L., Ding, X.L., & Lu, Z. (2011a). *ISPRS Journal of Photogrammetry and Remote Sensing*, 66, 146-152

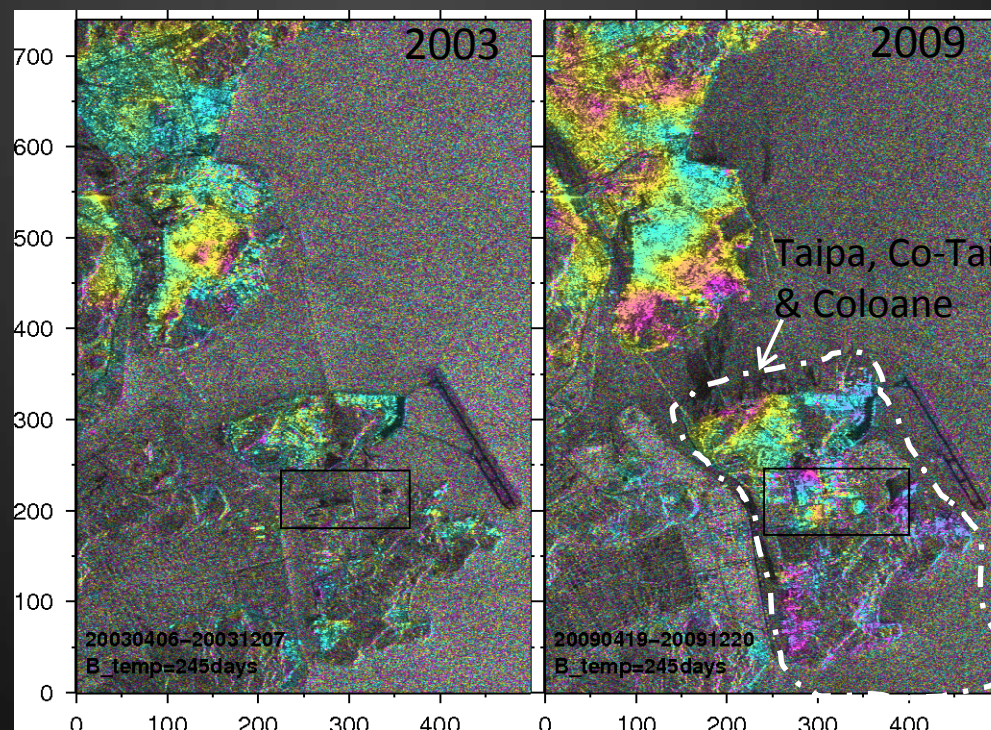
\*: Zhang, L., Ding, X.L., & Lu, Z. (2011b). *IEEE Transactions on Geoscience and Remote Sensing*, 49, 547-556

# Case studies: 1. Macau with C-band data



(Macau)

Data:  
38 Envisat/ASAR images acquired from  
**2003 to 2010**  
81 interf. selected with baseline  
thresholds: 250day, 150m and 300Hz



(Many buildings have been put up...)

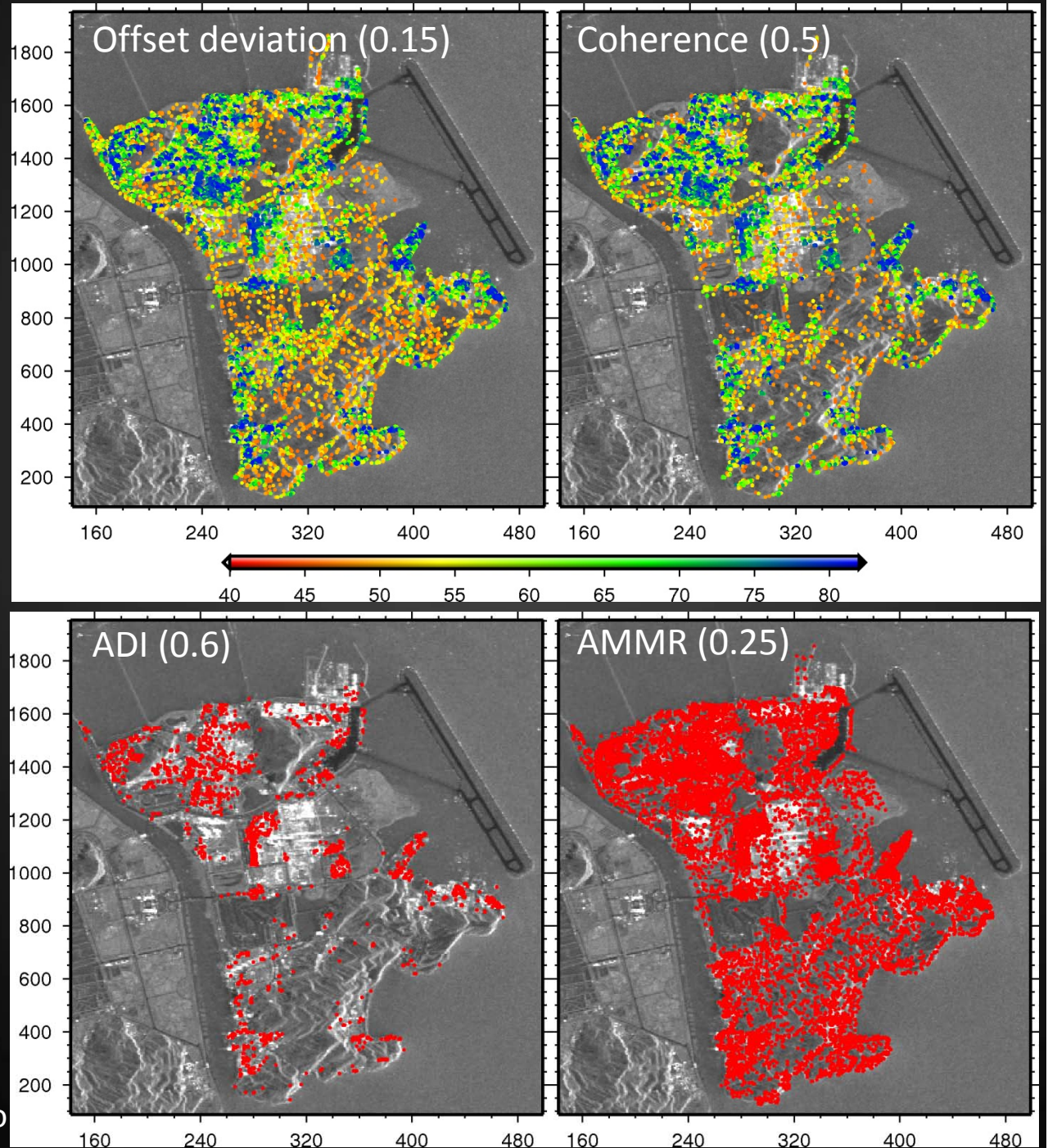
# Case studies

Image pair based methods:

TCP selection

Image based methods:

ADI: Amplitude Dispersion Index  
AMMR: Amplitude Mad Median Ratio

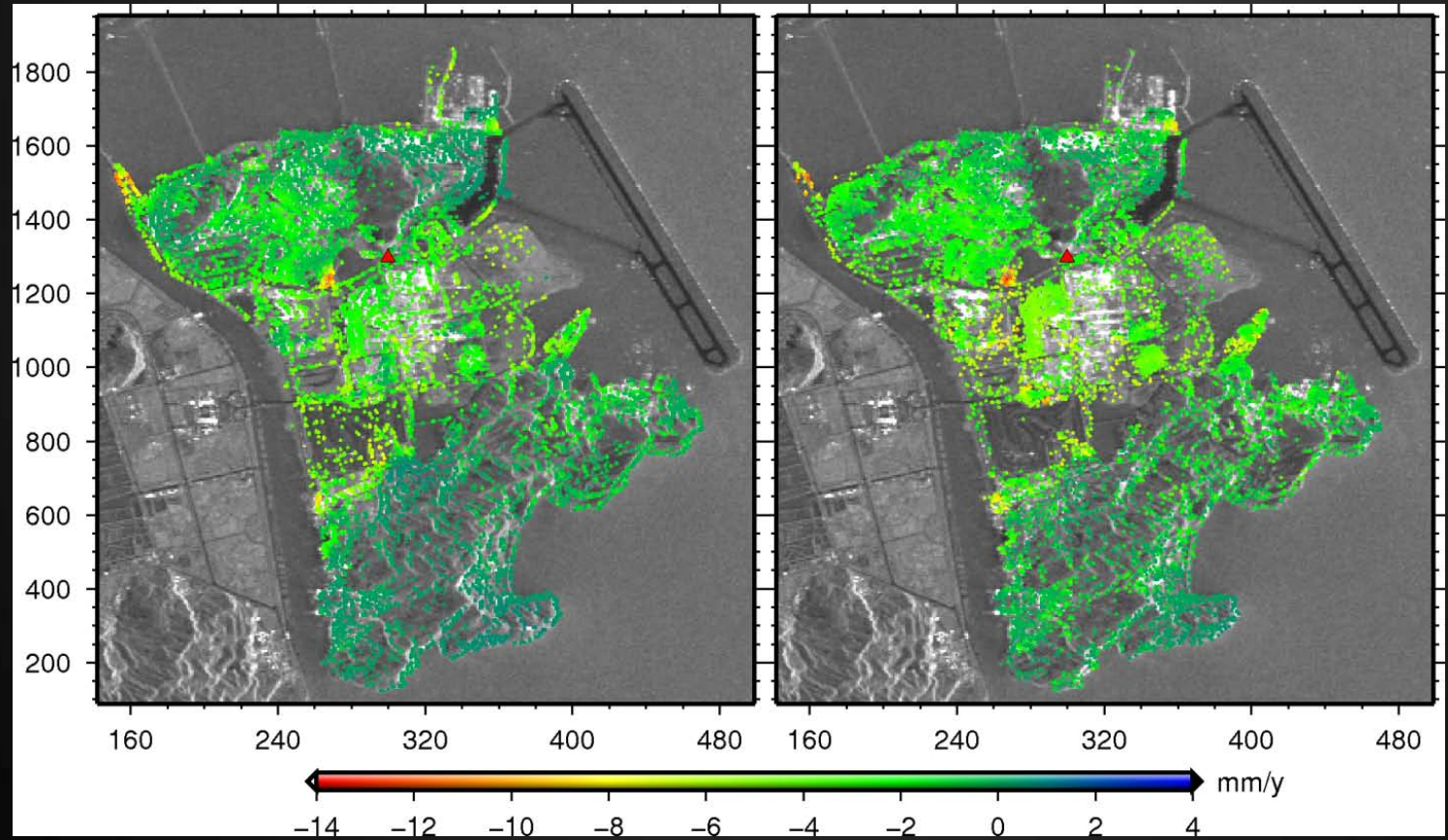


# Case studies

LS estimator on TCPs selected by offset deviation

L-1 norm estimator on TCPs selected by AMMR

Result  
s



Consistent with ground measurements provided by DSCC of Macau

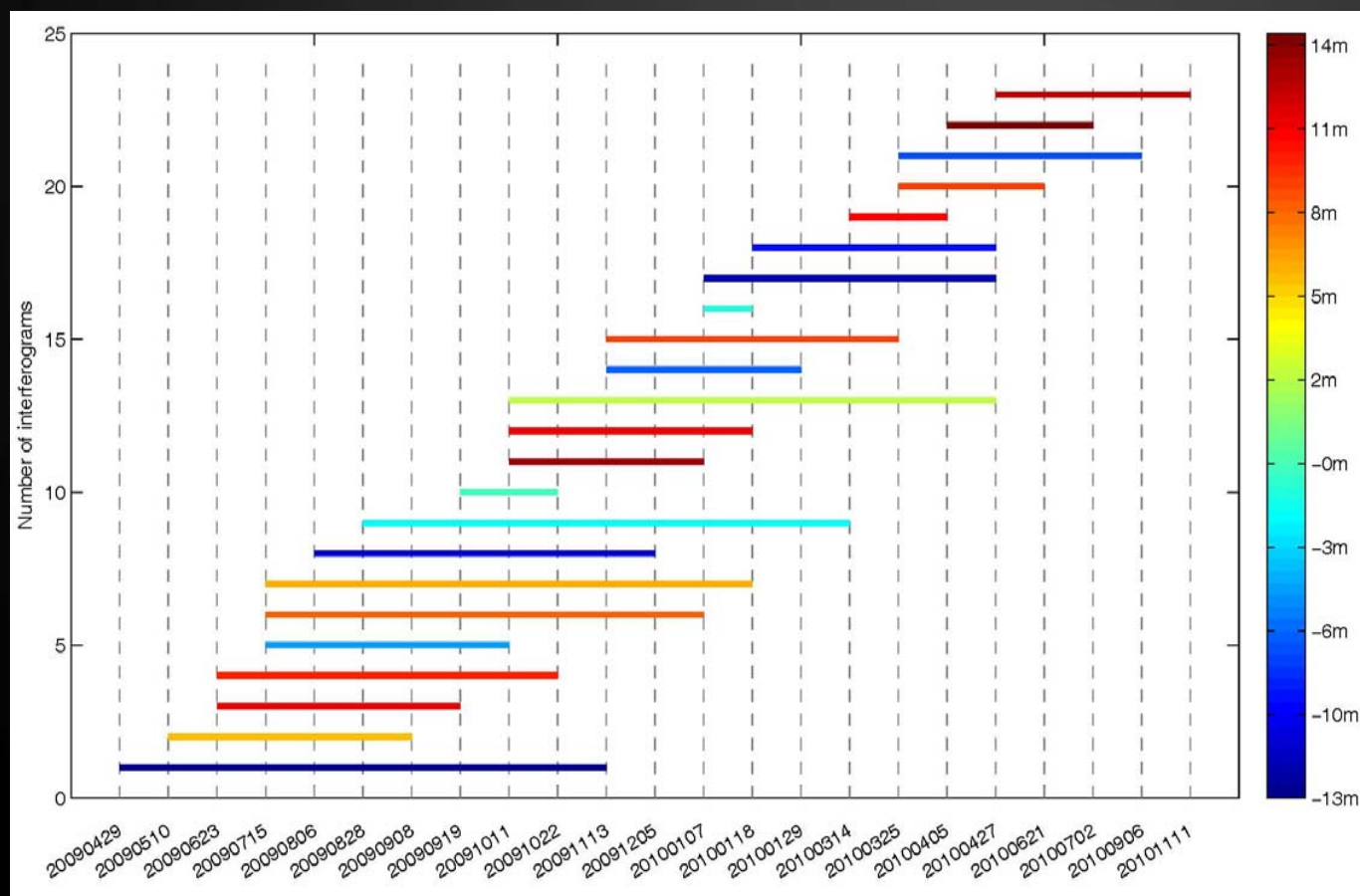


## Case studies: 2. Tianjin with X-band data

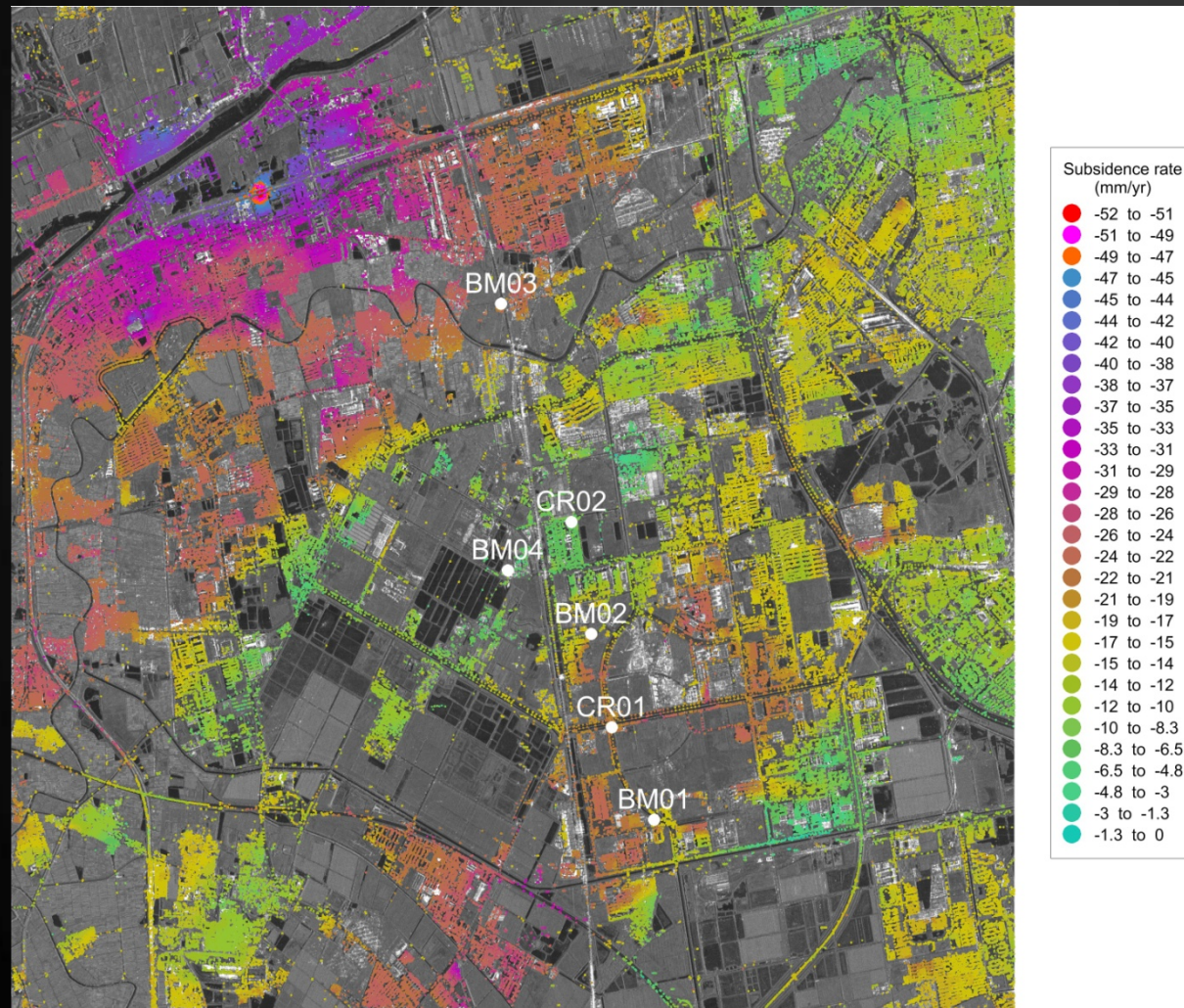
TerraSAR-X: High resolution (3m-by-3m)

External DEM: Low resolution (90m)

Ultra short baselines!!

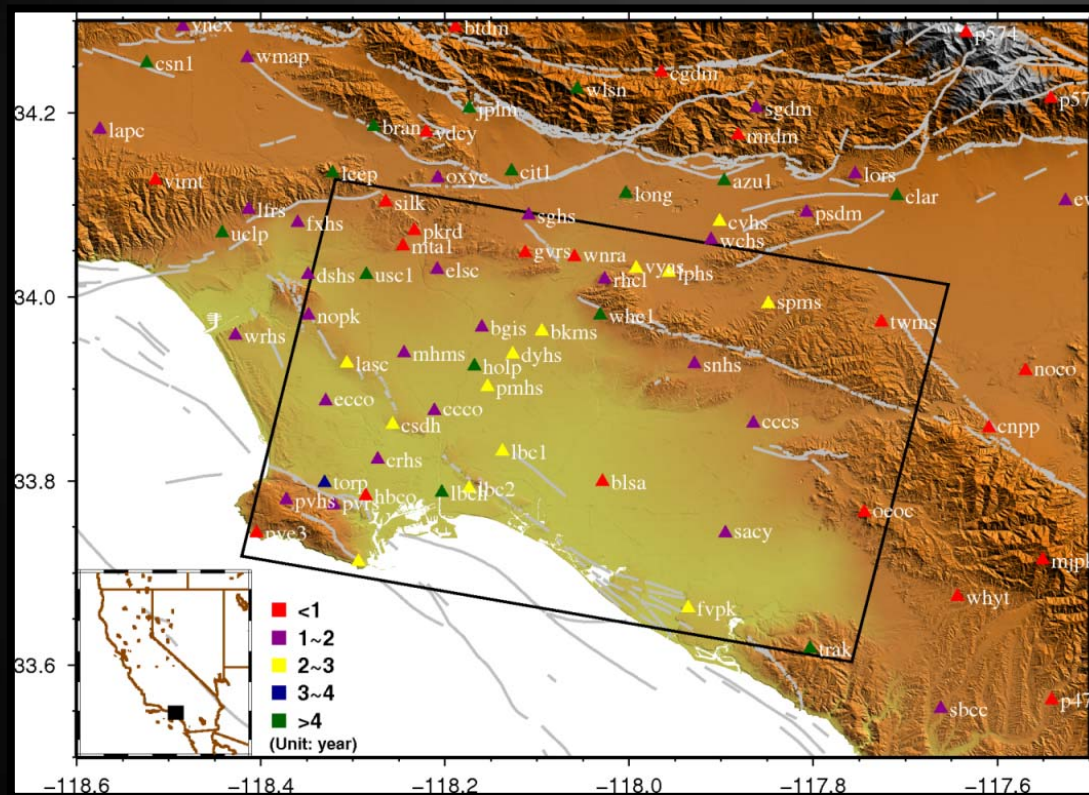


## Case studies: 2. Tianjin with X-band data



Mean defo. rate over Tianjin from 2009 to 2010

## Case studies: 3. LA basin with C-band data



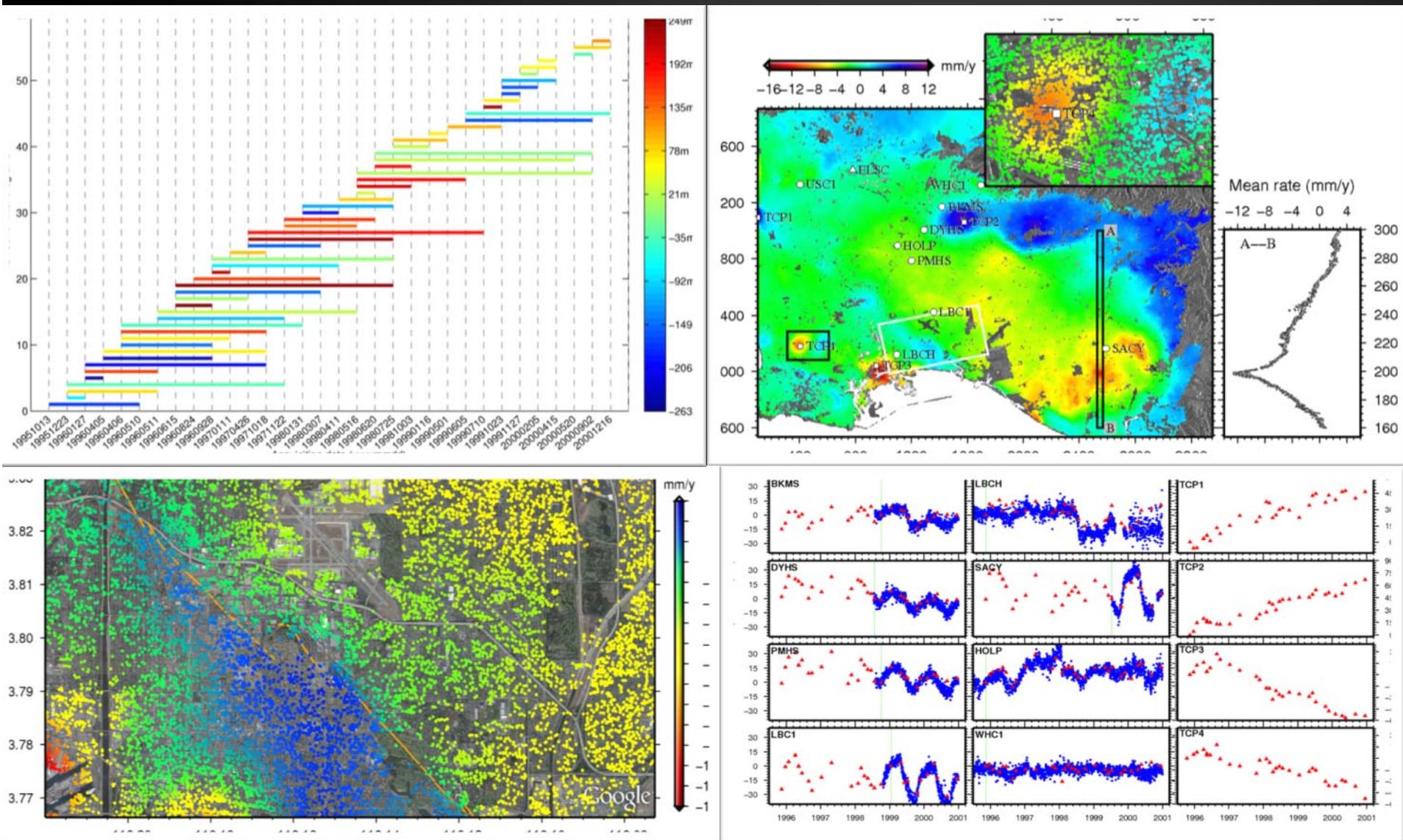
55 interferograms from 32

ERS-1/2 images

Baseline threshold:

300m;2.5yr;300Hz

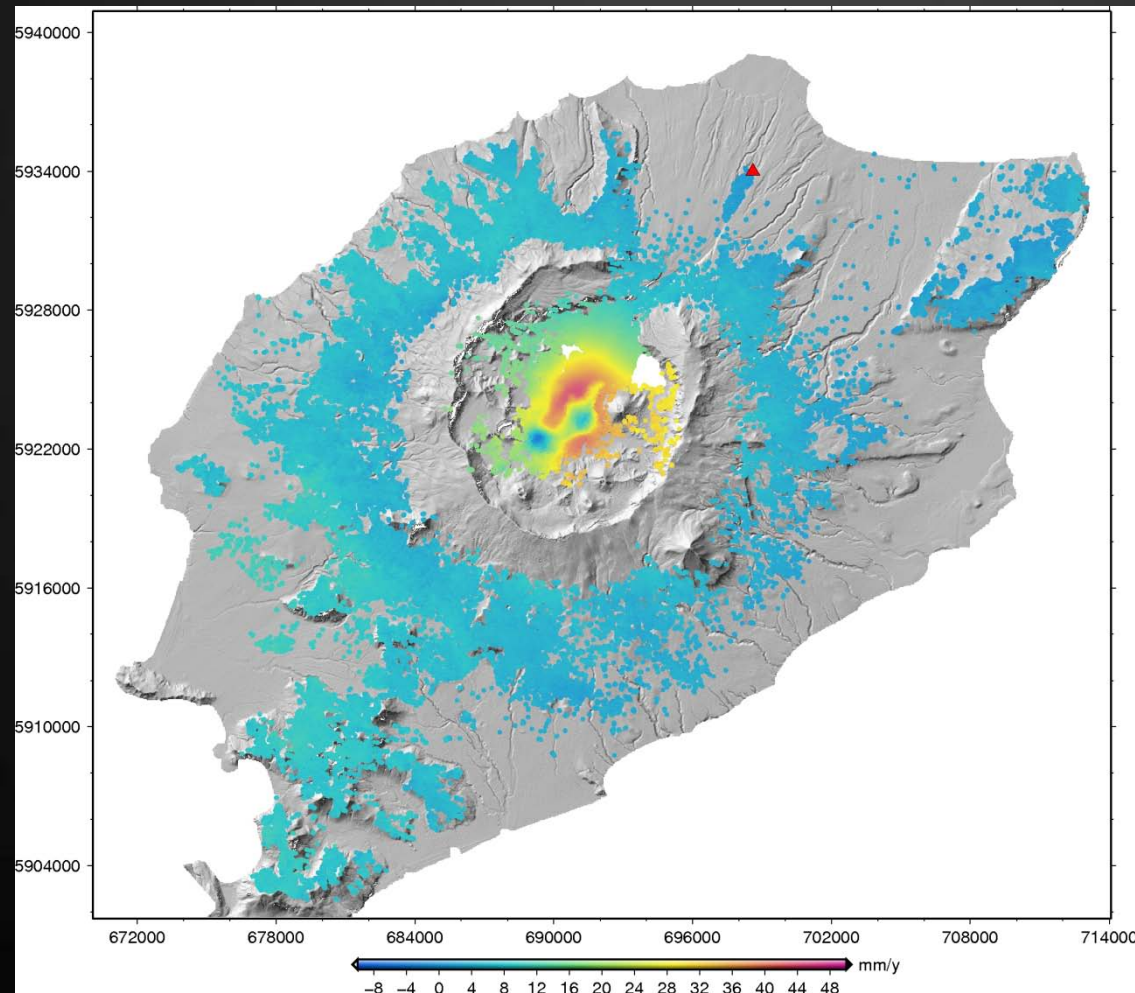
# Case studies: 3. LA basin with C-band data



# Case studies: 3.Okmok volcano with C-band data

24 interferograms with spatial baseline less than 300m and temporal baseline less than 700d constructed from 19 **Envisat/ASAR images**

Mean defo. rate  
20030610-20080708



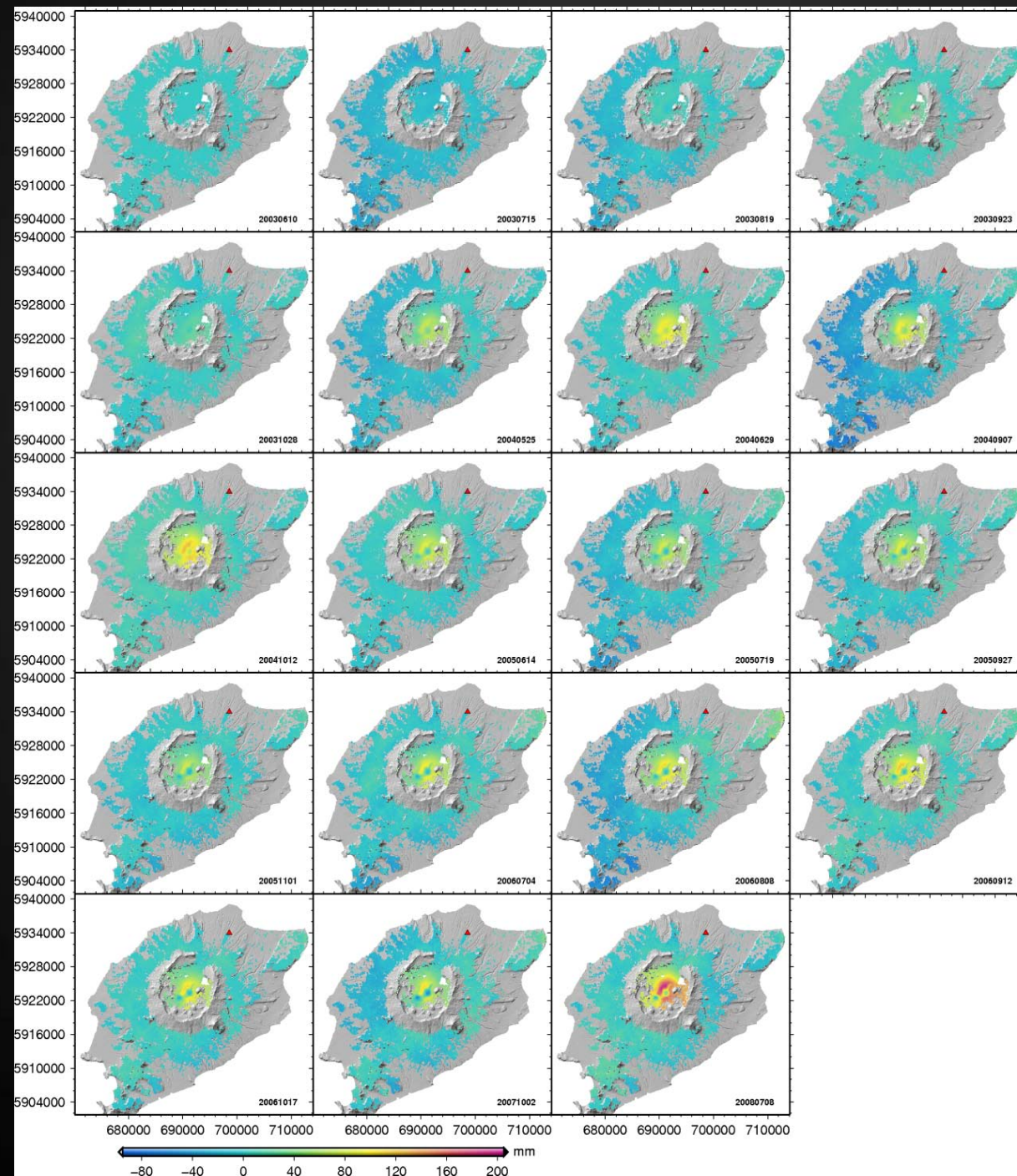
# Okmok: deformation time series

20030610

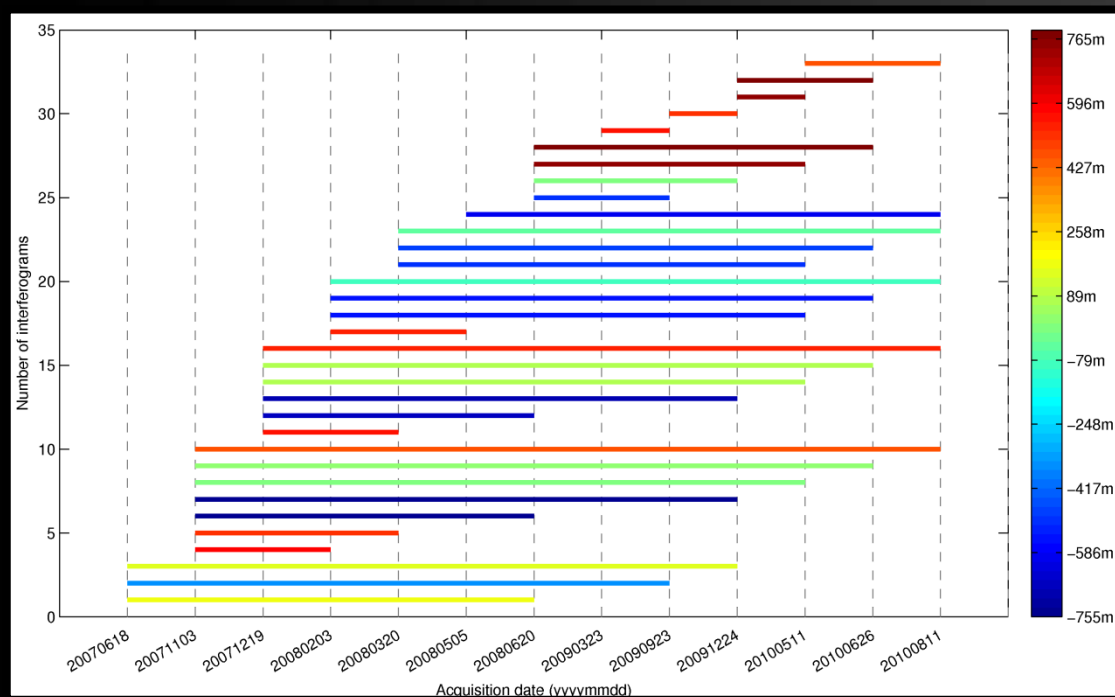


20080708

Eruption:  
20080712



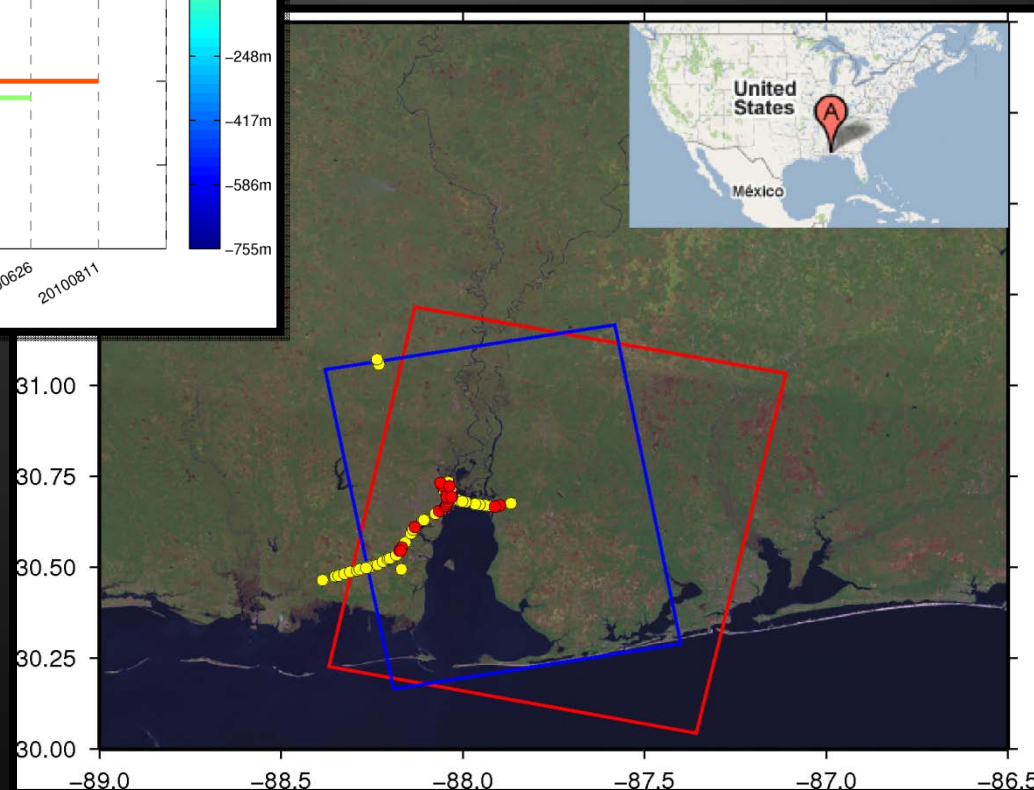
# Case studies: 4. Mobile city with L-band data



ALOS/PALSAR data

19 interferograms generated from 12 SAR images.

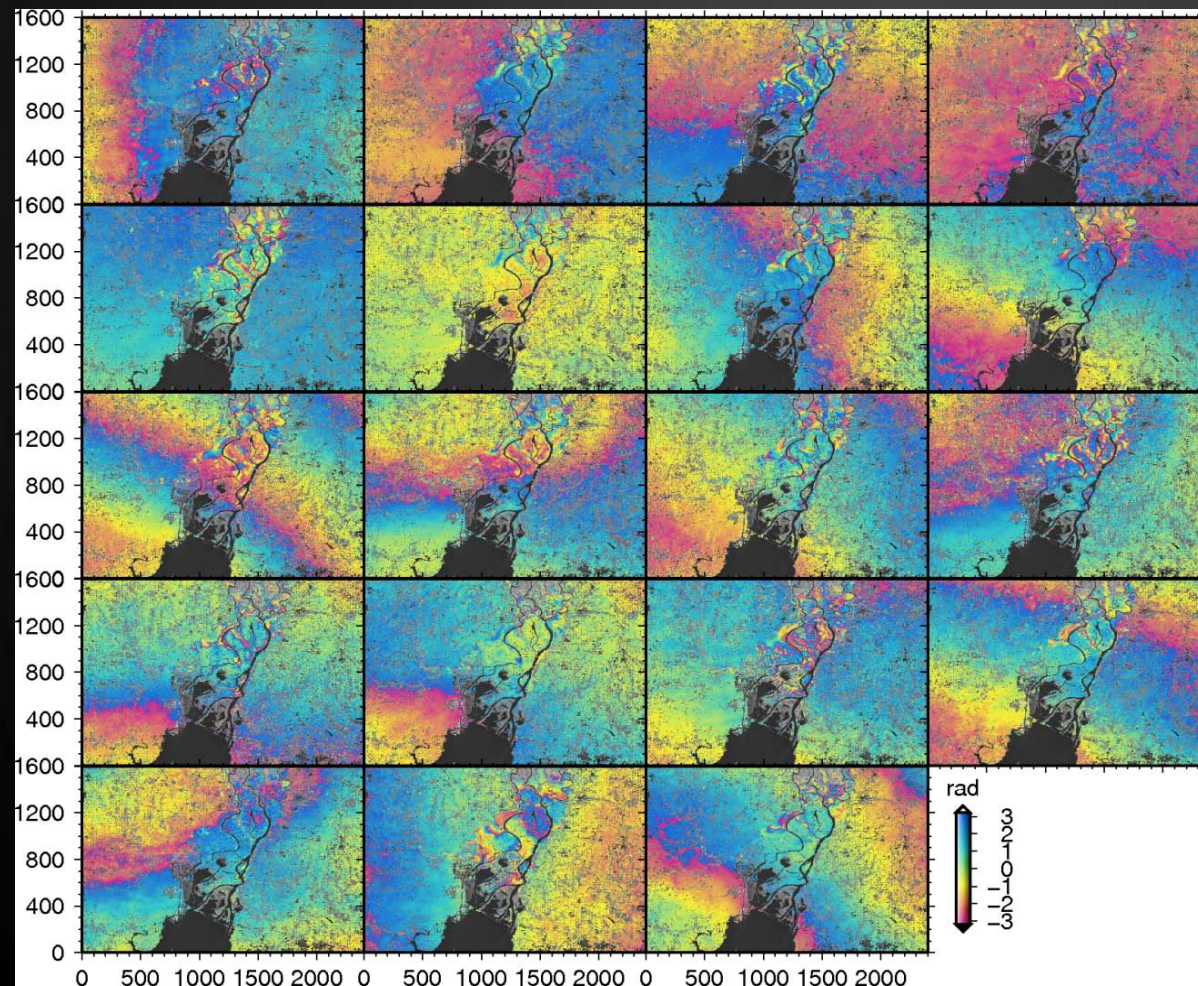
422,440 TCPs and 1,444,800 arcs



# Case studies: 5. Mobile city with L-band data

Solution: TCPIInSAR (v2.0)

---Resolving the deformation parameters together with orbital errors!

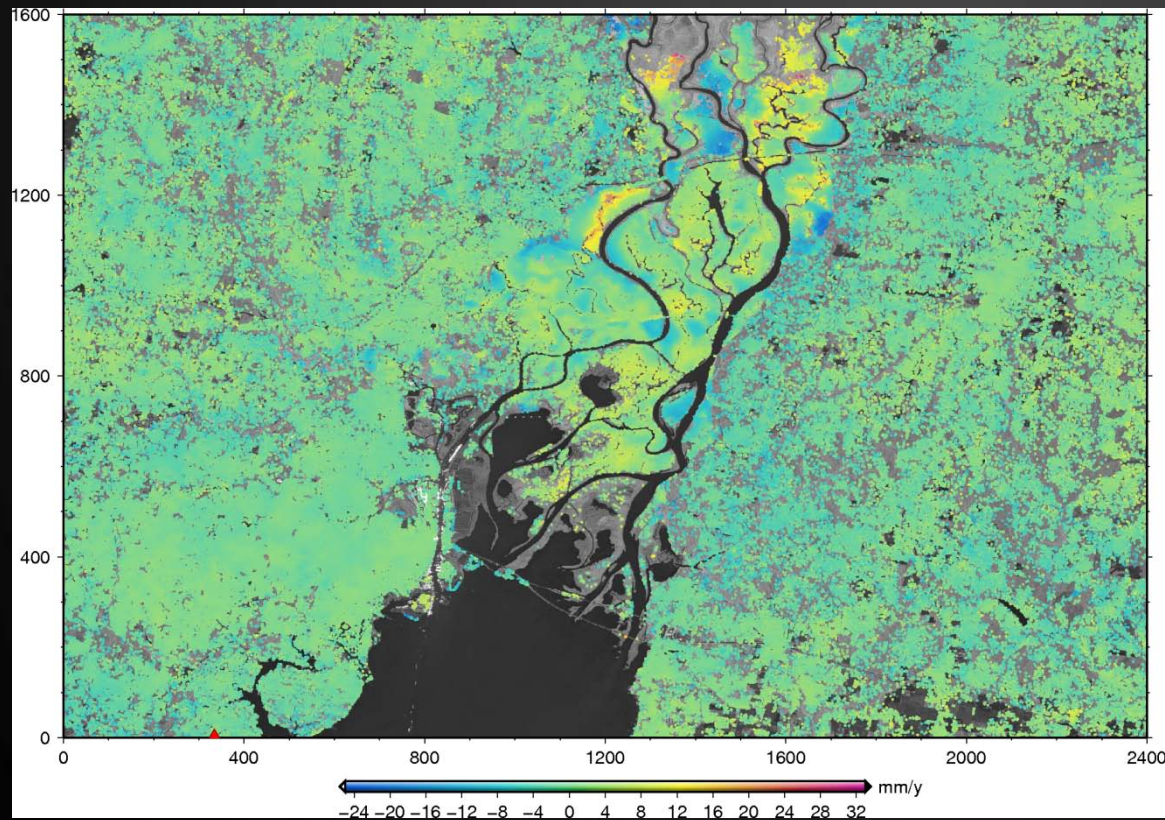




## Case studies: 5. Mobile city with L-band data

Solution: TCPIInSAR (v2.0)

---Resolving the deformation parameters together with orbital errors!

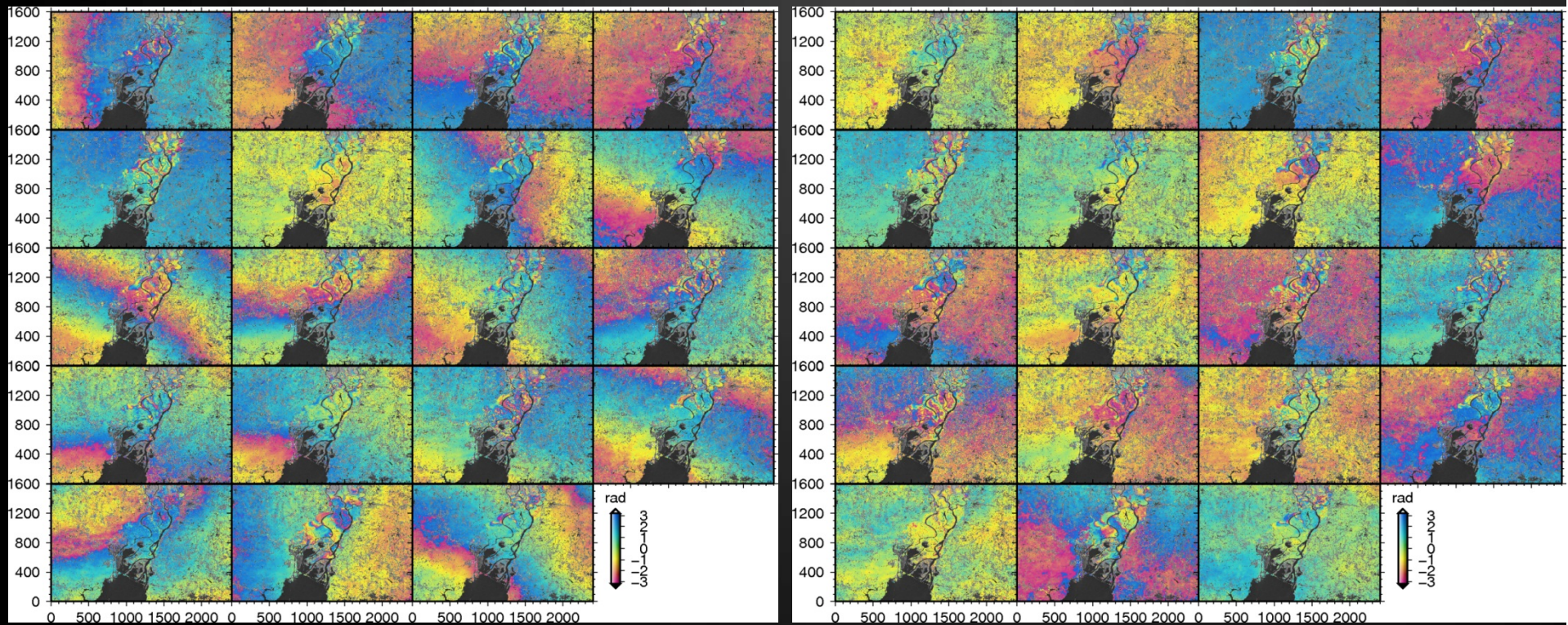


Mean defo. rate (2007-2010)

# Case studies: 5. Mobile city with L-band data

Solution: TCPIInSAR (v2.0)

---Resolving the deformation parameters together with orbital errors!



# Conclusion

TCPIInSAR is a promising tool for deformation monitoring on changing landscapes with multi-temporal SAR images.

- TCPIInSAR can identify both **persistently** and **partially coherent points**
- TCPIInSAR can estimate linear deformation rate (for partially coherent points) and deformation time series (for persistently coherent points) **with no need of phase unwrapping**
- TCPIInSAR (v2.0) can estimate deformation rate and orbital errors simultaneously
- TCPIInSAR(v2.0) can estimate ground deformation without external DEM
- **Deformation time series over Hong Kong?**  
Reclaimed areas, infrastructures ...  
Lack of funding for ordering SAR data...

Thanks!  
Questions?

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[lu@usgs.gov](mailto:lu@usgs.gov)

# Temporarily Coherent Point InSAR

## TCP identification: Image based method

### Amplitude Mad-Median Ratio (AMMR)

Median absolute deviation  
 $\text{Mad}(X) = \text{median}(\text{abs}(X - \text{median}(X)))$

$$\sigma_v \cong \frac{\sigma_A}{m_A} \rightarrow \sigma_v \cong \frac{\text{Mad}_A}{\text{Median}_A}$$

A point with scaled intensity time series (25): **PS? No; TCP? Yes!**

[0.1, 0.2, 0.2, 0.3, 0.2, 0.2, 0.3, 0.8, 0.85, 0.9, 0.9, 0.92, 0.92, 0.91, 0.94, 0.93, 0.95, 0.95, 0.92, 0.94, 0.92, 0.91, 0.91, 0.92, 0.93];

$$\sigma_v \cong \frac{\sigma_A}{m_A} = 0.45 \quad \sigma_v \cong \frac{\text{Mad}_A}{\text{Median}_A} = 0.03$$

We do not know in which interferogram the selected TCPs are coherent.

# Temporarily Coherent Point InSAR

## TCP Parameter Estimator

- To resolve DEM error and linear deformation rate **without the need of phase unwrapping**
- Observations are **differential phases at the arcs** (point pairs) in **multi-master interferograms with short baselines**
- Core algorithms:

**L-2 norm (least squares) estimator with ambiguity detector[5]**

**L-1 norm estimator**

[5] Zhang, L., Ding, X.L., & Lu, Z. (2011b). *IEEE Transactions on Geoscience and Remote Sensing*, 49, 547-556

# Temporarily Coherent Point InSAR

## The system of observations

$$\phi_{l,m}^i = \phi_{topo,l,m}^i + \phi_{defo,l,m}^i + \phi_{atmo,l,m}^i + \phi_{orbit,l,m}^i + \phi_{noise,l,m}^i$$

For each arc, we have

$$\phi_{defo,l,m}^i = -\frac{4\pi}{\lambda} \Delta r_{l,m}^i = -\frac{4\pi}{\lambda} \sum_{j=S_i+1}^{M_i} (t_j - t_{j-1}) v_j$$

$$= \beta_i V$$

$$\phi_{topo,l,m}^i = -\frac{4\pi}{\lambda} \frac{B_{\perp,l,m}^i}{r_{l,m}^i \sin \theta_{l,m}^i} \Delta h_{l,m}$$

$$= \alpha_{l,m}^i \Delta h_{l,m}$$

Wrapped phases!!

$$\Delta \Phi = A \begin{bmatrix} \Delta h_{l,m,l',m'} \\ \Delta V \end{bmatrix} + W$$

$$\Delta \Phi = [\Delta \phi_{l,m,l',m'}^1 \quad \Delta \phi_{l,m,l',m'}^2 \quad \cdots \quad \Delta \phi_{l,m,l',m'}^I]$$

$$A = [\alpha \quad \beta]$$

$$\alpha = [\alpha_{l,m}^1 \quad \alpha_{l,m}^2 \quad \cdots \quad \alpha_{l,m}^I]^T$$

$$\beta = [\beta_1 \quad \beta_2 \quad \cdots \quad \beta_I]^T$$

$$W = [w_{l,m,l',m'}^1 \quad w_{l,m,l',m'}^2 \quad \cdots \quad w_{l,m,l',m'}^I]$$

$$\Delta \phi_{l,m,l',m'}^i = \alpha_{l,m}^i \Delta h_{l,m,l',m'} + \beta_i \Delta V + w_{l,m,l',m'}^i$$

$$w_{l,m,l',m'}^i = \Delta \phi_{atmo,l,m,l',m'}^i + \Delta \phi_{orbit,l,m,l',m'}^i + \Delta \phi_{noise,l,m,l',m'}^i$$

How to resolve the parameters?

# Temporarily Coherent Point InSAR

## L-2 norm (least squares) estimator with ambiguity detector

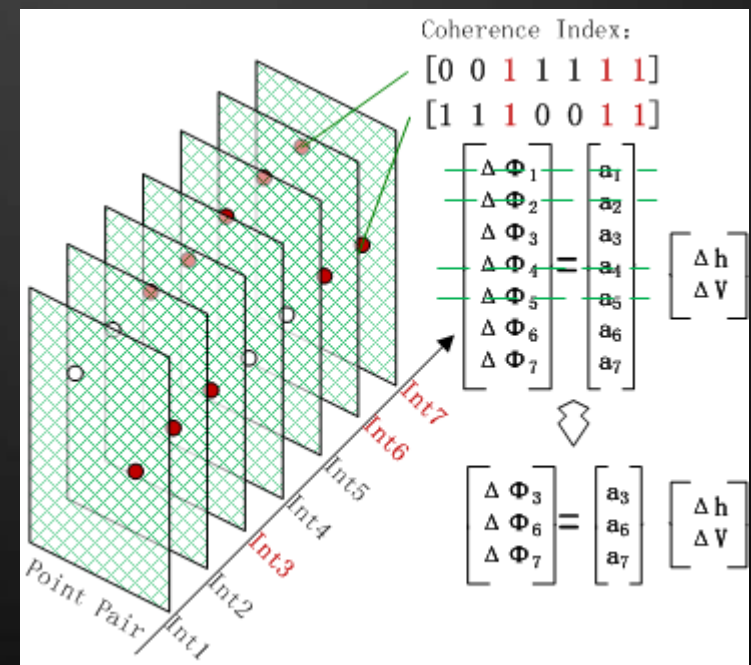
- This algorithm is suitable for TCPs identified by **image-pair** based methods
- Since we exactly know in which interferograms the selected TCPs keep high coherence, we can get a coherence index for each TCP
- For each arc, only interferograms in which both points keep coherent are selected.

$$\begin{bmatrix} \Delta \hat{h}_{l,m,l',m'} \\ \Delta \hat{V} \end{bmatrix} = (A^T P^{dd} A)^{-1} A^T P^{dd} \Delta \Phi$$

$$\Delta \hat{\Phi} = A (A^T P^{dd} A)^{-1} A^T P^{dd} \Delta \Phi$$

$$r = \Delta \Phi - A (A^T P^{dd} A)^{-1} A^T P^{dd} \Delta \Phi$$

$\Delta \Phi$  might have phase ambiguities!!





# Temporarily Coherent Point InSAR

L-2 norm (least squares) estimator with ambiguity detector

 Ambiguity detector

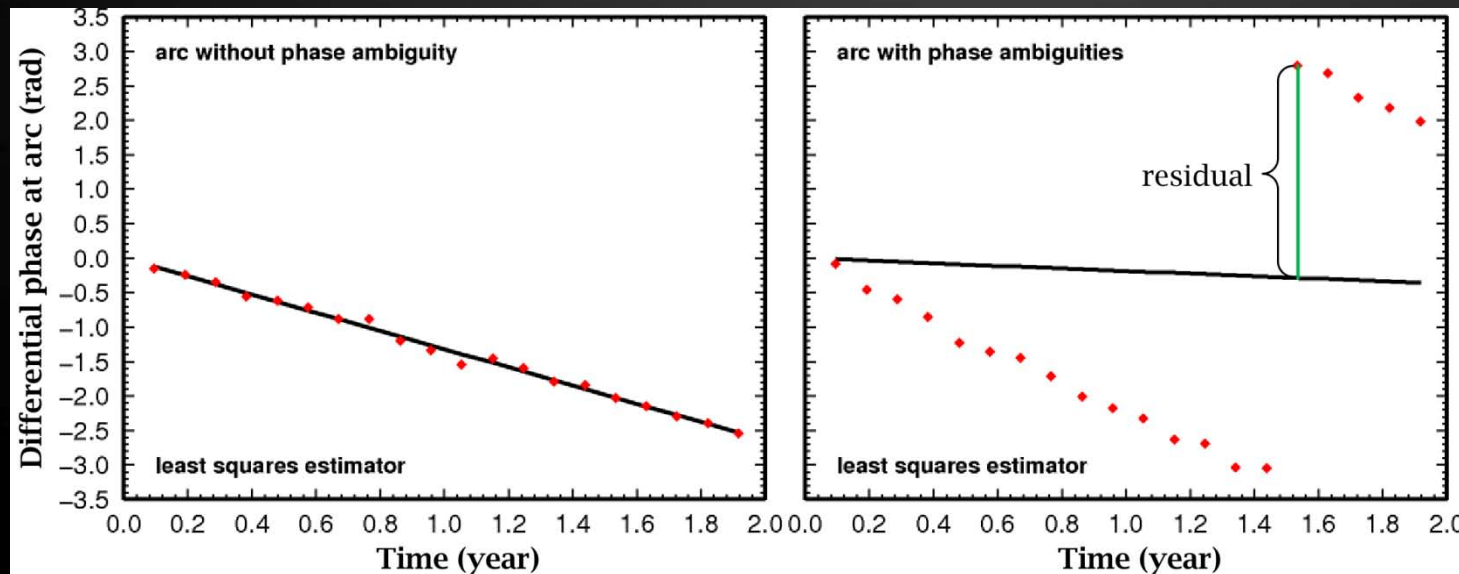
$$Q_{\Delta\hat{\phi}\Delta\hat{\phi}} = A(A^T P^{dd} A)^{-1} A^T$$

$$\text{Max}(|r_i|) > c\sqrt{\text{Max}((Q^{dd})_{ii})} + 2\sqrt{\text{Max}((Q_{\Delta\hat{\phi}\Delta\hat{\phi}})_{ii})}$$

 TCP parameters

After removing modulo-2pi arcs,  
perform Arc-Point integration

LS residuals can tell us whether the arc has ambiguity or not!



# Temporarily Coherent Point InSAR

## L-1 norm estimator

- For TCPs selected by **image based** approach, **we do not exactly know** in which interferograms the TCPs are coherent
- When taking all interferograms as observations, we need to design **a robust estimator** to suppress the effect of “outliers” (i.e., decorrelated phases and phase ambiguities at arcs)
- **L-1 norm estimator** is a good choice since it is **less sensitive to outliers** than LS

With L-1 norm estimator, we do not need to remove arcs having decorrelated phases and phase ambiguities!!

# Temporarily Coherent Point InSAR

## L-1 norm estimator

- How to perform L-1 norm estimation?

L-1 norm estimator is to find  $\hat{x}$  as follows:

$$\hat{x} = \arg \min_x \|b - Ax\|_1$$

$$\Delta\Phi = A \begin{bmatrix} \Delta h_{l,m,l',m'} \\ \Delta V \end{bmatrix} + W \quad \Rightarrow \quad \text{minimize } \sum_i \left| \Delta\phi_{l,m,l',m'}^i - \sum_j A_{ij} \begin{bmatrix} \Delta h_{l,m,l',m'} \\ \Delta V \end{bmatrix} \right|$$

- Solution by iteratively reweighted least squares used in [6] for robust SBAS
- Solution by linear programming**

[6] Lauknes, T. R., Zebker, H.A. and Larsen Y. (2011). IEEE Transactions on Geoscience and Remote Sensing, 49, 536-546

# Temporarily Coherent Point InSAR

L-1 norm estimator: Solution by linear programming

$$\text{minimize } \sum_i \left| \Delta \phi_{l,m,l',m'}^i - \sum_j A_{ij} \begin{bmatrix} \Delta h_{l,m,l',m'} \\ \Delta V \end{bmatrix} \right|$$



$$\text{minimize } \sum_i f_i$$

$$\text{subject to } f_i - \left| \Delta \phi_{l,m,l',m'}^i - \sum_j A_{ij} \begin{bmatrix} \Delta h_{l,m,l',m'} \\ \Delta V \end{bmatrix} \right| = 0$$



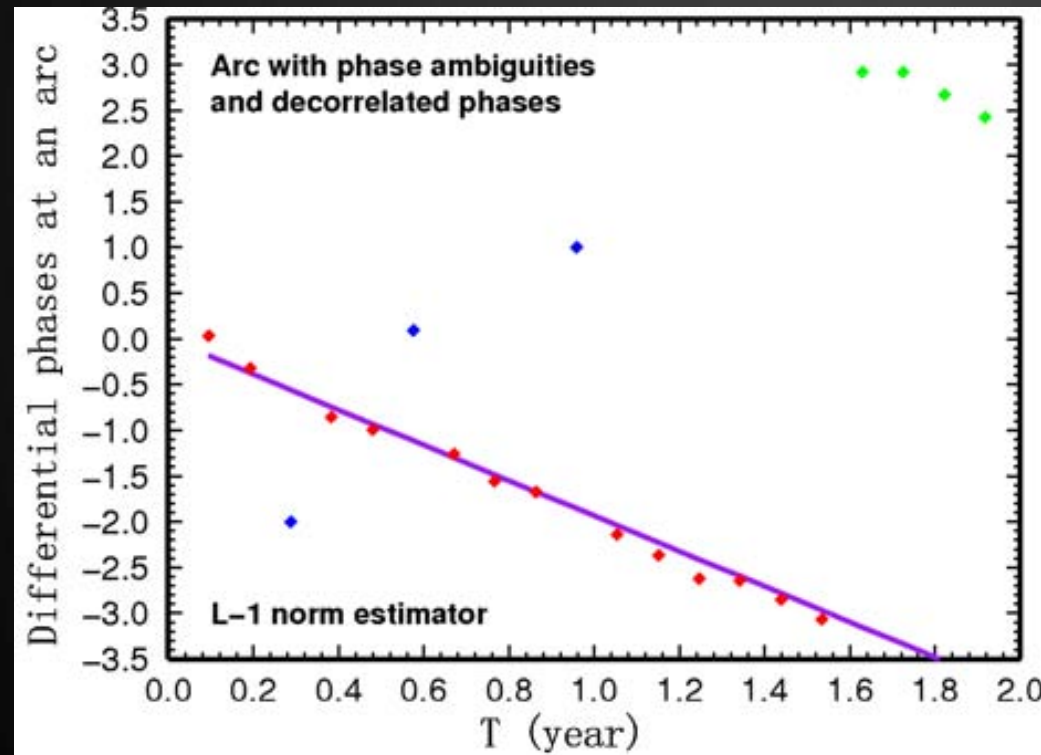
$$\text{minimize } \sum_i f_i$$

$$\text{subject to } -f_i \leq \Delta \phi_{l,m,l',m'}^i - \sum_j A_{ij} \begin{bmatrix} \Delta h_{l,m,l',m'} \\ \Delta V \end{bmatrix} \leq f_i$$

With any linear programming software package, it can be solved easily.

# Temporarily Coherent Point InSAR

The performance of the L-1 norm estimator?



Even though the arc contains decorrelated phases as well as phase ambiguities, the L-1 norm estimator can precisely resolve the defo. rate!